# Non-stationary Autoregressive Model for On-line Detection of Inter-area Oscillations in Power Systems

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- Power Systems Monitoring. Problem Statement
- State-of-the-art Techniques
- Stabilized Forgetting Approach for On-line Oscillations Detection
- Key Steps of the Proposed Algorithm
- Testing on Simulated Data
- Testing on Real World Data (500kV Power Grid)
- Conclusions

### Detailed modelling of oscillations

Factors influencing oscillations:

- the position of the subsystem in the whole power system.
- the distribution of the natural damping elements such as series resistance of the lines, and shunt resistance of the loads.
- the number and position of special damping controllers.

### Blind oscillation detection

- all variables are monitored on-line,
- oscillation is a result of unknown cause,
- detection algorithm is designed to warn the operators as early as possible.

# State-of-the-art Techniques

the observed process is locally approximated by a linear system

- locality: window shapes (square, triangle, exponential).
- Parameters of the linear system are estimated
  - Kalman filter: requires the noise variance to be known
  - RLS: variance can be estimated
- oples of the system are computed from the estimates
  - typically only the point estimates are considered
- stability and oscillatory behavior is analyzed
  - setting thresholds on closeness to stability border

Our approach:

- Exponential window
- Q Autoregressive model with unknown variance
- Full posterior density on parameters
- Probability of stabable poles computed

## Model of the signal

### Model

$$y_t = a_t y_{t-1} + b_t y_{t-2} + c_t + \sigma_t e_t$$
 (1)

where  $y_t$  is the observed signal,  $a_t, b_t, c_t, \sigma_t$  are its unknown parameters, and  $e_t$  is Gaussian noise with zero mean and unit variance,  $e_t = \mathcal{N}(0, 1)$ . which defines PDF of the observed random variable  $y_t$ :

$$p(y_t|y_{t-1}, y_{t-2}, a_t, b_t, \sigma_t) = \mathcal{N}(a_t y_{t-1} + b_t y_{t-2}, \sigma^2).$$
(2)

#### Bayesian treatment

- Estimation of time-invariant system is RLS (Gauss-inverse-Wishart posterior).
- Can be extended to time-invariant system by model of parameter evolution
- Alternatively, we may choose to model the parameters as random walk, leading to a method known as forgetting.

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Regularized exponential forgetting is formalized as follows:

$$p(a_t, b_t, \sigma_t | y_1, \dots, y_t) \propto p(y_t | y_{t-1}, y_{t-2}, a_t, b_t, \sigma_t) \ imes p(a_{t-1}, b_{t-1}, \sigma_{t-1} | y_1, \dots, y_{t-1})^{\phi} \ imes ar{p}(a_{t-1}, b_{t-1}, \sigma_{t-1} | y_1, \dots, y_{t-1})^{1-\phi}.$$

Here,  $\bar{p}(\cdot)$  denotes an *alternative* probability of the parameters. It preserves posterior density of the Normal-inverse-Gamma type,

$$p(a_t, b_t, \sigma_t) = \mathcal{N}i\mathcal{G}(V_t, \nu_t), \tag{4}$$

the statistics of which are as follows:

$$V_t = \phi V_{t-1} + [y_t, y_{t-1}, y_{t-2}, 1]' [y_t, y_{t-1}, y_{t-2}, 1] + (1 - \phi) \bar{V},$$
(5)

and  $\nu_t = \phi \nu_{t-1} + 1 + (1 - \phi) \overline{\nu}$ . Here,  $\overline{V}, \overline{\nu}$  denote statistics of the alternative pdf.

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(3)

## Probability of oscilations

The poles of the system are:

$$p_{1,2} = \frac{a_t \pm \sqrt{a_t^2 + 4b_t}}{2}$$

The system is oscillating when:

$$a_t^2 < -4b_t$$

and the system is unstable when  $\left| p_{1,2} \right| > 1$ , i.e.

$$|p_{1,2}| = \left| \left( rac{a_t}{2} 
ight)^2 - rac{a_t^2 + 4b_t}{4} 
ight| = |b_t| > 1.$$



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Key Steps of the Algorithm:

**Off-line**: choose initial alternative statistics,  $\bar{V}, \bar{\nu}$  and forgetting factor  $\phi$ . **On-line**: at each time *t* do:

- update statistics  $V, \nu$ ,
- **2** compute posterior marginal estimates of parameters  $\hat{a}_t$ ,  $\hat{b}_t$ , var(a), var(a),
- Occupation compute probability of unstable oscillations as follows

$$Pr(unstab.oscil.) = Pr(a_t < 2)Pr(b_t < -1)$$
$$= \frac{1}{2} \left( 1 - \operatorname{erf} \frac{\hat{a}_t - 2}{\sqrt{2} \operatorname{var}(a_t)} \right) \frac{1}{2} \left( 1 - \operatorname{erf} \frac{\hat{b}_t + 1}{\sqrt{2} \operatorname{var}(b_t)} \right) \quad (6)$$

## Simulation studies



- Area 1 and Area 2 are sending and receiving subsystems accordingly.
- From 50 to 115 second, increase of active power output of G2 from 500 MW to 660 MW. Active power increase rate 2.5 MW per second;
- From 165 to 230 second, decrease of active power output of G2 from 660 MW to 500 MW. Active power decrease rate 2.5 MW per second.
- Bus 8 is monitored.

# Simulation studies



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## Real data



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### Oscillation detection algorithm is based on autoregressive model

- universal black-box model for oscillations
- Ø more detailed modelling would yield more informative models
- allows estimation of the noise variance
- o forgetting factor is the only tuning parameter

### Statistical approach

- full posterior density is evaluated, posterior risk of oscillations
- 2 allows hypotheses testing: what is more likely cause of oscillations
- o more detailed modelling of the forgetting factor is being developed